

# **Method for Protecting Public Key Schemes from Timing, Power and Fault Attacks**

5

## **BACKGROUND OF THE INVENTION**

### **1. Field of the Invention**

10       The present invention generally relates to make a number-theoretic public key scheme and more particularly, a scheme for protecting public key from timing, power monitoring and fault attacks.

### **2. Description of the Prior Art**

15

      In conventional cryptosystems, cryptographic algorithm is derived from mathematical models. It makes people believe it is impossible to extract secret key with a low complexity algorithm. However some problems caused during cryptographic implementations are not  
20       considered within mathematical models and what allows attacks to find out the secret keys via some indirect techniques such like microprobing, reverse engineering, memory read-out techniques, etc. To prevent these attacks, a variety of physical techniques for protecting cryptographic devices are known, including enclosing key management



systems in physically durable enclosures, coating integrated circuits with special coatings that destroy the chip when removed, and wrapping devices with fine wires that detect tampering. However, these approaches are difficult to use in single-chip solutions (such as smartcards), and difficult to evaluate since there is no mathematical basis for their security. Physical tamper resistance techniques are also ineffective against some attacks.

In the past five years, it has shown that attackers can non-invasively extract secret keys using careful measurement and analysis of many devices' power consumption. Analysis of timing measurements or electromagnetic radiation can also be used to find secret keys.

Many public-key encryption algorithms, like the RSA encryption and decryption system or the Diffie-Hellman key exchange system, are based on the mathematical operation of modulo exponentiation. This operation can be described as follows:

$$C = M^e \bmod n.$$

In other words, to compute C, raise M to the power of e and divide it by n, then save the remainder of the division instead of the quotient. In a typical RSA calculation, M would be the clear text message to be signed, e would be the private key, n would be the public key (the



modulus), and  $C$  would be the ciphertext.

Modulo calculations, or synonymously, modular calculations, can be performed by electronic equipment. As the exponent,  $e$ , and the ciphertext,  $M$ , and size of  $n$  increases, the modulo calculations become  
5 time and power consuming to the electronic circuits. Generally, computation time depends on the size of  $n$  and the value of  $e$ . In hardware, circuits that implement modulo mathematics,  $n$  and  $e$  also provide an indication of the amount of power consumed by the circuit  
10 while performing the operation.

As mentioned above,  $n$  is publicly known as a public key, but  $e$  could be a private key that should be kept secret in order to maintain the integrity of the encryption system. In order to calculate  $C$ , it is  
15 useful to break the modulo exponentiation up into a multiple of simple operations. Usually, the modulo exponentiation is split up into a series of modulo-square and modulo-multiplication operations. "Modulo" in this context means division by the modulus while saving the remainder of the operation.

20

According to "Paul C. Kocher in his paper, Timing attacks on implementations of Diffie-Hellman, RSA, DSS, and other systems, Proceedings of Crypto '96, 1996", and "Paul C. Kocher in his paper, Kocher, Cryptanalysis of Diffie-Hellman, RSA, DSS, and other systems



using timing attacks, Dec. 7, 1995", some information about the cryptographic key leak out by measuring the length of cryptographic computation.

5        When modulo mathematics is performed, the computation is generally performed using binary numbers, from most significant (MSB) to least significant (LSB), i.e., from left to right, and performing the modulo computation described in FIG.1. As shown in FIG.1, notice that each time a 1 is encountered then a modulo-square (line 3) is performed with the intermediate result, which is initialized to a 1, and then a modulo-multiply with M is performed (line 5). When a 0 is encountered only a modulo-square is performed (line 3) on the intermediate result to get the next intermediate result. Thus, depending on whether the condition of line 4 was satisfied (a 1 or a 0 was present in a position in the private key, e exponent), it may take different amounts of time to calculate the next intermediate result. Thus, the attacker may first observe a set of operations while measuring the time (t) taken to compute each  $C = M^e \bmod n$  and find out what the secret key is.

20

Another attack available to an attacker is to monitor the power consumption of the integrated circuit. Generally, the modulo math calculation of a modulo-multiply and a modulo-square will each require a different amount of energy when implemented in either



hardware or firmware in an integrated circuit. When implement a modulo-multiply, it will have power peak wider than implement a modulo-square. An attacker could monitor the power consumption of an integrated circuit to determine the exponent  $e$ .

5

When 1 is encountered (a modulo-square is performed with the intermediate result, and then a modulo-multiply with  $M$  is performed), it will show a narrow power peak followed by a wide power peak in the power consumption trace. When 0 is encountered (only a modulo-square is performed on the intermediate result to get the next intermediate result), it will only show a narrow power peak in the power consumption trace. According to power consumption of FIG.2, we can find out that the secret key is 00111.

10

As the aforementioned, operation of modulo-multiplication or modulo-squaring occurs at any particular time is controlled by a conditional jump (line 4 in FIG.1) that depends on the value of the exponent,  $e$ , as it is traversed, commonly bit-by-bit. Based on this simple theory, there is an improved cryptographic algorithm which is shown in FIG.3. This algorithm reduces leakage from cryptosystems by implementing critical operations using fixed execution path routines whereby the execution path does not vary in any manner that can reveal useful information about the secret key during subsequent operations so as to protect cryptographic keys against timing attacks

15

20



and power monitoring attacks.

Due to the advanced attack techniques, there are more and more new approaches to attack cryptosystem, some techniques used to prevent attacks in the past were not strong enough to provide protection against new attacks anymore. According to “Sung-Ming Yen, Seung-Joo Kim, Seon-Gan Lim, and Sang-Jae Moon. A Countermeasure against One Physical Cryptanalysis May Benefit Another Attack. Information Security and Cryptology-ICISC 2001, volume 2288 of Lecture Notes in Computer Science, pages 414-427. Springer-Verlag, 2002”, there is a fault attack technique called “C safe error”. And there’s still another fault attack called “M safe error” which is proposed by “Sung-Ming Yen and Marc Joye. Checking Before Output May Not Be Enough against Fault-Based Cryptanalysis. IEEE Trans. On Computers, 49(9): 967-970, September 2000”. It will be shown that the cryptographic algorithms in FIG.3 can not immune from C safe error attacks or M safe error attacks.

Fault attacks try to introduce errors into the cryptographic computation, and to identify the key by analyzing the mathematical and statistical properties of the erroneously computed results. Among the many techniques that suggested so far for introducing such errors are the uses of ionizing radiation, unusual operating temperatures, power and clock glitches, and laser-based chip microsurgery.



C safe-error attacks introduce temporal error within ALU so as to induce temporal erroneous computation. Some of the attacks carry out an erroneous computation, while others won't. Upon these different outputs, some information of the cryptographic key will be revealed. In FIG.3, when some  $e_k = 0$ ,  $S_b = (S_b \cdot S_2) \bmod n$  is a redundant computation. It is to say that if a temporal error is introduced during this computation, it will induce an erroneous computation but this erroneous result will not affect the next computation cycle, so the final output will still be the same. If the attacker introduce a single error at a random time during the computation of  $S_b = (S_b \cdot S_2) \bmod n$ , by observing whether the output of the computation is with error or not, the attacker can realize the corresponding bit of the secret key. If the output is with error, the corresponding digit of the secret key is 1; otherwise, the corresponding digit of the secret key is 0.

As for the M safe-error attack, suppose we have an operation  $Y=(X \cdot Y) \bmod n$  which means after the computation of  $X \cdot Y \bmod n$ , the result is reassigned to register Y. In the modular computation, both X and Y are with very long digits (for example 1024 bits), and regular CPU only can do multiplication with 32 bits, so multiplicator will be separated into 32 blocks with 32 bits in each block. Therefore the multiplication of X and Y will be computed separately such as  $Y_0=(X \cdot Y_0) \bmod n$ ,  $Y_1=(X \cdot Y_1) \bmod n$ , ...,  $Y_{31}=(X \cdot Y_{31}) \bmod n$ . Therefore, if one or several bits



of error are introduced into the more significant bit positions of register, no error will be detected after restoring the result into Y if the faulty bits belonging to the block  $Y_i$  are no longer required. If we change the operation into  $Y=(Y \cdot X) \bmod n$ , as aforementioned, if an error is introduced in block  $X_j$ , then register X is not cleared and the final value will be incorrect. With the temporary error, the attacker can realize the corresponding bit of the secret key. If the output is with error, the corresponding bit of the secret key is 0; otherwise, the corresponding bit of the secret key is 1.

10

The algorithm provided by FIG.3, if  $e_k = 1$ , it needs to calculate  $S_0 = (S_2 \cdot S_0) \bmod n$ . If an attacker uses C safe-error attack and a temporary error is introduced during this computation, it will cause an erroneous result in  $S_0$ . And this erroneous result  $S_0$  will affect the next computation cycle, so the final output will be incorrect. If the attacker introduces a single error at a random time during the computation of  $S_b = (S_2 \cdot S_b) \bmod n$ , by observing whether the output of the computation is with error or not, the attacker can realize the corresponding bit of the secret key. If the output is with error, the corresponding bit of the secret key is 1; otherwise, the corresponding bit of the secret key is 0.

20

In accordance with the above description, a new and improved cryptographic algorithm which can protect secret keys from timing attacks, power attacks, C safe-error attacks and M safe-error attacks is



therefore necessary.

## **SUMMARY OF THE INVENTION**

5        In accordance with the present invention, a novel cryptographic algorithm is provided that substantially overcomes the drawbacks of the above mentioned problems.

10        Accordingly, it is one object of the present invention to provide protective techniques without conditional jump in the modular exponentiation algorithm for public key schemes, which provide strong protection against the described timing and power monitoring attacks.

15        It is another object for present invention to provide a modular exponentiation algorithm without any redundant calculation in it so as to be substantially immune from both C safe-error attack.

20        It is still another object for present invention to provide a modular exponentiation algorithm for public key schemes without any store operation having non-certain destination so as to prevent the M safe-error attack intended to determine a private key.

In according to the foregoing objectives, the present invention



provides a method for protecting public key schemes from timing, power and fault attacks. In general, this is accomplished by implementing critical operations using "branchless" or fixed execution path routines whereby the execution path does not vary in any manner that can reveal new information about the secret key during  
5 subsequent operations. More particularly, the present invention provides a modular exponentiation algorithm without any redundant computation so that it can protect the secret key from C safe-error attacks. The improved method also provides an algorithm that doesn't  
10 have a store operation with non-certain destination so that the secret key is immune from M safe error attacks. Furthermore, in the modulo exponentiation algorithm, the times of the multiplication doesn't change resulting from different exponentiations for protecting from timing attack.

15

This invention provides a method, an apparatus or a computer-readable medium for protecting public key schemes from timing, power monitoring and fault attacks comprising the steps of: 1. obtaining a message for use in a cryptographic operation; 2.  
20 obtaining a modulus and an exponent corresponding to said cryptographic operation, wherein said exponent contains at least one bit; 3. initializing a first value as a one, and assigning the message to a second value; 4. executing a modulo exponentiation



algorithm on each bit of the exponent from a most significant bit to a least significant bit, wherein the algorithm comprising the steps of: a. input a bit to an inverter and storing the output as a third value, and assigning the next bit of the exponent as a fourth value; b. if the third value is a zero, updating the first value with the result of squaring, modulo the modulus the first value, if the third value is a one, updating the first value with the result of multiplying, modulo the modulus said first value by the second value; and c. if the fourth value is a zero, updating the first value with the result of squaring, modulo the modulus the first value, if the fourth value is a one, updating the first value with the result of multiplying, modulo the modulus the first value by the second value; 5. updating the bit with the next bit of the exponent, and executing steps of the algorithm on the bit until the bit being the least significant bit of the exponent; and 6. storing and output the first value.

## **BRIEF DESCRIPTION OF THE DRAWINGS**

The foregoing aspects and many of the attendant advantages of this invention will become more readily appreciated as the same becomes better understood by reference to the following detailed description, when taken in conjunction with the accompanying drawings, wherein:



FIG.1 shows the modular exponentiation algorithm of  $C = M^e \bmod n$ ;

FIG.2 shows the power consumption diagram of algorithm from FIG.1;

5

FIG.3 shows the modular exponentiation algorithm of  $C = M^e \bmod n$  which is immune from both timing attacks and power monitoring attacks;

10 FIG.4 shows the algorithm which is immune from fault attacks;

FIG.5 shows the flow chart of the algorithm from FIG.4; and

FIG.6 shows the comparison table of the algorithm from FIG.1 and FIG.

15 4 when exponent is 10001100.

## **DESCRIPTION OF THE PREFERRED EMBODIMENT**

Referring now to the drawings, preferred embodiments will now be  
20 described in detail. Since public key schemes and computer hardware and software implementation are well known to those of skill in the art, no description of same is deemed necessary to a full, concise, and exact understanding of the present invention.



Those skilled in the art will recognize that the algorithm in FIG.1 describes one commonly used conventional procedure for computing  $R=M^e \bmod n$ , where “^” denotes exponentiation. As will be inherently understood to those skilled in the art, the base M is the message, e is exponent, and n is modulus. As aforementioned, the procedure in FIG.1, security is compromised if an attacker can determine whether or not the device actually performed the modular multiplication step  $S=(S \cdot M) \bmod n$  because this determines whether the k-th bit of the exponent e is one or zero. By monitoring the occurrence of modular multiplication as exponentiation occurs on a bit-by-bit basis, the exponent can therefore be determined.

The novel protective technique for public key schemes which provide strong protection against the described timing attacks, power monitoring attacks, and more particularly against C safe-error attacks and M safe-error attacks will now be described. Moreover, not only the RSA public key schemes, but also any system on the basis of discrete logarithm can be employed with the algorithm of the present invention.

The present invention provides an algorithm as in FIG.4. At the beginning, obtaining a message M for use in a cryptographic operation and an exponent  $e=(e_{w-1}, e_{w-2}, \dots, e_1, e_0)$  and a correlated



modulus  $n$  then initializing  $S_0=1$ , assigning  $M$  to  $S_1$ , and let  $e_{-1}=1$  (100), then set  $k=w-1$  and executing a modulo exponentiation algorithm on each bit of the exponent from the most significant bit ( $e_{w-1}$ ) to the least significant bit ( $e_0$ ), wherein the algorithm comprising the steps of: **1.**

5 Input the bit  $e_k$  to an inverter and storing the output as a value  $b$ , and assigning the next bit  $e_{k-1}$  as a value  $c$ ; **2.** Executing  $S_0=(S_0 \cdot S_b) \bmod n$  and  $S_0=(S_0 \cdot S_c) \bmod n$  (130) **3.** Executing  $k=k-1$  (140); **4.** Repeating step 1 to step 3 until finishing the loop of  $k=0$ ; **5.** Storing and output  $S_0$  (150).

10

Next, we will illustrate the correctness of the present invention. FIG.6 shows the comparison of two algorithms provided by FIG.1 and FIG.4 when the exponent with standard binary representation "10001100". In order to execute two calculations in each iteration, as

15 shown in FIG.6, the algorithm in FIG.4 calculates the  $S=(S \cdot S) \bmod n$ , which belongs to the second digit  $e_k=0$ , one iteration ahead. Due to the pre-calculation of the  $S=(S \cdot S) \bmod n$ , the remaining calculation  $S=(S \cdot M) \bmod n$  will be postponed to the next iteration. If the procedure of **1.**  $S=(S \cdot M) \bmod n$ ; **2.**  $S=(S \cdot S) \bmod n$  is changed to calculate  $S=(S \cdot S) \bmod n$

20 first, based on the mathematical derivation, the following  $S=(S \cdot M) \bmod n$  should be calculated twice in order to get the same result. Therefore, if we pre-calculate  $S=(S \cdot S) \bmod n$ , then the previous procedure should become **1.**  $S=(S \cdot S) \bmod n$ ; **2.**  $S=(S \cdot M) \bmod n$ ; **3.**  $S=(S \cdot M) \bmod n$ .



In the beginning, during the seventh iteration  $e_7=1$ , the calculations of " $S=(S_0 \cdot S_0) \bmod n$ " and " $S=(S_0 \cdot S_c) \bmod n$ " where  $c=e_6$  will be executed. Therefore, during the seventh iteration, the calculations should be " $S=(S_0 \cdot S_0) \bmod n$ " and " $S=(S_0 \cdot S_0) \bmod n$ " in turn within  
5 which the first calculation of " $S=(S_0 \cdot S_0) \bmod n$ " is an original procedure but the second calculation of " $S=(S_0 \cdot S_0) \bmod n$ " is pre-calculated due to  $e_6=0$ .

The next iteration is the sixth iteration where  $e_6=0$ , and the  
10 calculations of " $S=(S_0 \cdot S_1) \bmod n$ " and " $S=(S_0 \cdot S_c) \bmod n$ " where  $c=e_5$  will be executed. Therefore during the sixth iteration, the calculations should be " $S=(S_0 \cdot S_1) \bmod n$ " and " $S=(S_0 \cdot S_0) \bmod n$ " in turn within which the first " $S=(S_0 \cdot S_1) \bmod n$ " is an original procedure, but the second calculation of " $S=(S_0 \cdot S_0) \bmod n$ " is pre-calculated due to  $e_5=0$ .  
15 The calculation of " $S=(S_0 \cdot S_1) \bmod n$ " which should have been done twice in row in this iteration is only executed once, so there is still one " $S=(S_0 \cdot S_1) \bmod n$ " left, and due to the second calculation " $S=(S_0 \cdot S_0) \bmod n$ " is performed first so the remaining one " $S=(S_0 \cdot S_1) \bmod n$ " should be calculated twice in the next row.

20

The following fifth iteration  $e_5=0$  executes the same procedures as the sixth loop so we will not describe the detail here.

The next iteration is the fourth iteration where  $e_4=0$ , and the



calculations of " $S=(S_0 \cdot S_1) \bmod n$ " and " $S=(S_0 \cdot S_c) \bmod n$ " where  $c=e_3$  will be executed. Therefore, during the fourth iteration, the calculations should be " $S=(S_0 \cdot S_1) \bmod n$ " and " $S=(S_0 \cdot S_1) \bmod n$ " in turn which just make up for the remaining calculations left by the previous iteration.

5

The next iteration is the third iteration where  $e_3=1$ , and the calculations of " $S=(S_0 \cdot S_0) \bmod n$ " and " $S=(S_0 \cdot S_c) \bmod n$ " where  $c=e_2$  will be executed. Therefore, during the third iteration, the calculations should be " $S=(S_0 \cdot S_0) \bmod n$ " and " $S=(S_0 \cdot S_1) \bmod n$ " in turn which is the same as the algorithm provided by FIG.1.

10

The second iteration where  $e_2=1$  is the same as the seventh iteration, and the first iteration where  $e_1=0$  is the same as the sixth iteration.

15

As for the final iteration, the iteration zero with  $e_0=0$ , the calculations of " $S=(S_0 \cdot S_1) \bmod n$ " and " $S=(S_0 \cdot S_c) \bmod n$ " where  $c=e_{-1}$  will be executed. In this algorithm, we assume  $e_{-1}=1$ , so the calculations should be " $S=(S_0 \cdot S_1) \bmod n$ " and " $S=(S_0 \cdot S_1) \bmod n$ " which just make up for the remaining calculations left by the previous iteration.

20

As above mentioned, the present invention provides a method for protecting public key schemes from timing, power and fault attacks.



In general, this is accomplished by implementing critical operations using “branchless” or fixed execution path routines whereby the execution path does not vary in any manner that can reveal new information about the secret key during subsequent operations. More particularly, the present invention provides a modular exponentiation algorithm without any redundant computation so that it can protect the secret key from C safe error attacks. The improved method also provides an algorithm that doesn’t contain a store operation with non-certain destination so that the secret key is immune from M safe error attacks.

Although the present invention has been described in its preferred embodiment, it is not intended to limit the invention to the precise embodiment disclosed herein. Those who are skilled in this technology can still make various alterations and modifications without departing from the scope and spirit of this invention. Therefore, the scope of the present invention shall be defined and protected by the following claims and their equivalents.